

**Assignment 5:** Due Thursday 9th May at 5pm

Late assignments will not be accepted except by prior arrangement (for a good reason)

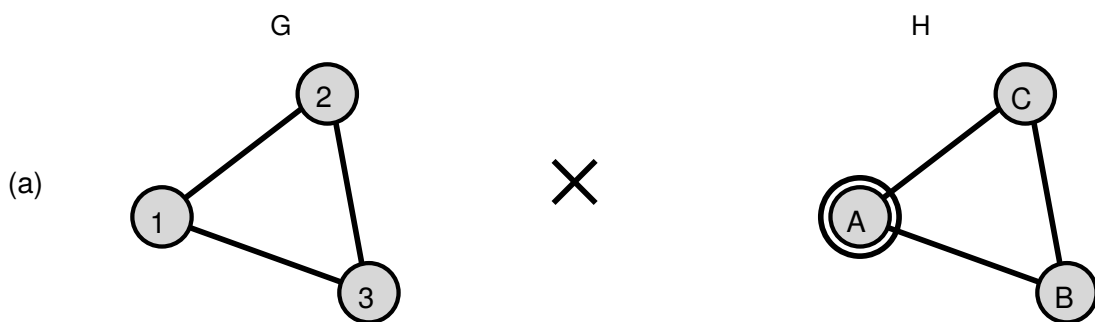
**Please include your student number in your handed up work, as Canvas doesn't give this to me automatically.**

1. Compute the following graph products

(i) Cartesian product

(ii) Rooted product

of the following pair of graphs (in the order given), where node *A* is the root of *H* where relevant.



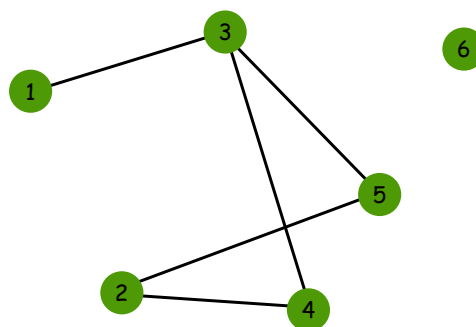
[2 marks]

2. Determine the maximum *k* such that the Cartesian product (above) is *k*-edge connected.

[2 marks]

3. Write code to derive the adjacency matrix of the line-graph  $L(G)$  of an undirected graph (input via its adjacency matrix).

Use your code to derive the degrees of the nodes of the line graph of the following graph. Please put your degrees in a table, where each node in the line graph is labelled by the edge it was derived from.



[3 marks]

4. Show that for a directed ring graph with *n* nodes and all edges pointing from node *i* to *i* + 1 mod *n* that  $A^{n+1} = A$  for adjacency matrix *A*.

[3 marks]